



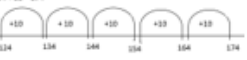

# Supporting Your Child with Maths





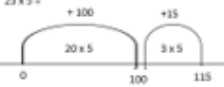
Parent Workshops Autumn Term 2023

# What Maths do we do?

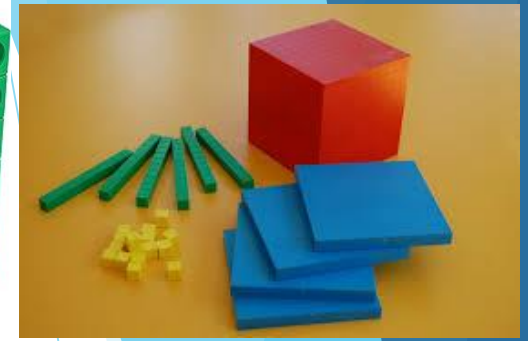
- ▶ Daily 1 hour maths lessons-covering all aspects of the maths national curriculum
- ▶ Followed by a daily, 20 minute additional maths session;
  - ▶ Mon: KIRF Session for all year groups
  - ▶ Tues, Wed, Thurs: Times Tables Workshops for Years 3 and 4
  - ▶ MMM (Maths Morning Meeting) for Years 5 and 6
  - ▶ Fridays: Arithmetic Session for all year groups

# Progression in Calculation

Year Group	Stage	Addition Strategy	Number Expectations																												
KS1 Year 3 Year 4 Year 5 Year 6	One	Real Life Concrete Resources  Socks, Fruit Pasta, Marbles Small toys etc.	Use real life objects to group objects to represent single digit numbers added to single digit numbers, for example 5 apples + 7 apples = 12 apples.																												
	Two	Concrete Mathematical Resources  Numicon Bead strings Straw bundles Dienes Place value counters	Use concrete materials to: Recall and use addition and subtraction facts up to 20. Derive related facts up to 100. Add three 1 digit numbers. Add pairs of 1 and 2 digit numbers Understand that addition is commutative. Concrete resources may also be used to support the introduction of the steps below.																												
	Three	Number lines for addition 	A three digit number and 1's, 10's and 100's Add two 2 digit numbers under 100. Add two 2 digit numbers totalling over 100.																												
	Four	Elegant number lines for addition 	Use elegant jumps to cross boundaries 10's, 100's, 1000's Use elegant number lines to support the development of mental methods. E.g. 678 + _____ = 1000																												
	Five	Expanded addition including carrying $345 + 218 = 563$ <table border="1" data-bbox="420 793 512 879"> <tr><td>H</td><td>T</td><td>O</td></tr> <tr><td>3</td><td>4</td><td>5</td></tr> <tr><td>2</td><td>1</td><td>8</td></tr> <tr><td>5</td><td>6</td><td>3</td></tr> </table>	H	T	O	3	4	5	2	1	8	5	6	3	Addition of two 2 digit numbers without carrying. Addition of a 2 digit and a 3 digit number without carrying. Addition of two 3 digit numbers without carrying. Addition of two 2 digit numbers with carrying into the tens. Addition of larger numbers up to two 3 digit numbers including carrying into the tens and into the hundreds.																
	H	T	O																												
	3	4	5																												
2	1	8																													
5	6	3																													
Six	Compact addition $3,458 + 1,322 = 4,780$ <table border="1" data-bbox="420 936 512 1022"> <tr><td>Th</td><td>H</td><td>T</td><td>O</td></tr> <tr><td>3</td><td>4</td><td>5</td><td>8</td></tr> <tr><td>+</td><td>1</td><td>3</td><td>2</td><td>2</td></tr> <tr><td>4</td><td>7</td><td>8</td><td>0</td></tr> </table>	Th	H	T	O	3	4	5	8	+	1	3	2	2	4	7	8	0	Compact addition should initially be shown alongside expanded addition. Addition of 2 digit and 3 digit numbers without carrying. Addition of 2 digit and 3 digit numbers carrying into the tens. Calculations which require carrying into the tens, hundreds, thousands and beyond. Calculations which require multiple times within a single calculation.												
Th	H	T	O																												
3	4	5	8																												
+	1	3	2	2																											
4	7	8	0																												
Seven	Compact addition with decimal places. $245.87 + 17.089 =$ <table border="1" data-bbox="420 1079 512 1165"> <tr><td>H</td><td>T</td><td>O</td><td>.</td><td>Th</td><td>Hd</td><td>Thd</td></tr> <tr><td>2</td><td>4</td><td>5</td><td>.</td><td>8</td><td>7</td><td>0</td></tr> <tr><td>+</td><td>0</td><td>1</td><td>7</td><td>.</td><td>0</td><td>8</td><td>9</td></tr> <tr><td>2</td><td>6</td><td>2</td><td>.</td><td>9</td><td>5</td><td>9</td></tr> </table>	H	T	O	.	Th	Hd	Thd	2	4	5	.	8	7	0	+	0	1	7	.	0	8	9	2	6	2	.	9	5	9	Calculations which involving numbers with up to 3 decimal places. Calculations which require carrying into the hundredths, tenths and one's column. Addition calculations where numbers are different sizes E.g. 3,467.02 + 85.089
H	T	O	.	Th	Hd	Thd																									
2	4	5	.	8	7	0																									
+	0	1	7	.	0	8	9																								
2	6	2	.	9	5	9																									

Year Group	Stage	Multiplication Strategy	Number Expectations
KS1 Year 3 Year 4 Year 5	One	Real Life Concrete Resources 	Use real life objects to group objects to represent single digit numbers multiplied by single digit numbers, for example 2 groups of 4 apples.
	Two	Concrete Mathematical Resources 	Use concrete mathematical resources to multiply single digit numbers by single digit numbers, for example 4 x 5.
	Three	Arrays 	Single digit x single digit e.g. 4 x 5 Multiples of ten x single digit e.g. 20 x 4 Teen numbers x single digit numbers, e.g. 16 x 5
	Four	Repeated Addition on a Number Line 	Single digit x single digit e.g. 4 x 5
	Five	Using known facts for multiplication If 3 x 4 is 12 3 x 40 = 120 30 x 40 = 1200	Derive related facts from known facts with appropriate size numbers for year group.
	Six	Partitioning (Number line) 	Teen numbers x single digit numbers, e.g. 16 x 5 Two digit numbers x single digit numbers e.g. 24 x 3
	Seven	Partitioning using mental methods $26 \times 4 = 144$ $20 \times 4 = 120$ $6 \times 4 = 24$ $120 + 24 = 144$	Multiply numbers mentally drawing upon known facts.
	Eight	Expanded Column Method $\begin{array}{r} 25 \\ \times 3 \\ \hline 75 \\ 20 \times 3 = 60 \\ \hline 75 \\ 150 \\ \hline 75 \\ 150 \\ \hline 150 \end{array}$	Two and three digit numbers x single digit numbers e.g. 145 x 5 Two digit number x two digit numbers e.g. 67 x 23
	Nine	Compact Column Method (Short Multiplication) $\begin{array}{r} 24 \\ \times 6 \\ \hline 144 \\ \hline 144 \\ \hline 144 \end{array}$	Two, three and four digit numbers x single digit numbers e.g. 2,145 x 5
	Ten	Long Multiplication $\begin{array}{r} 235 \\ \times 27 \\ \hline 1645 \\ 4700 \\ \hline 6345 \end{array}$	Two, three and four digit numbers x two digit numbers e.g. 235 x 27

# The CPA approach



The Concrete Pictorial Abstract (CPA) approach is a system of learning that uses physical and visual aids to build a child's understanding of abstract topics.

Concrete-KS1 and early KS2 but can continue further up where needed. Children use practical objects to help count and calculate, for example buttons, Dienes, counters, multi-link, real life objects, bead-strings, fraction tiles, Numicon etc

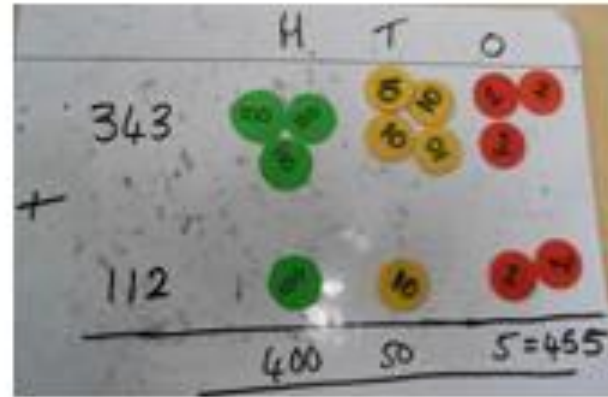
Pictorial-children draw pictures and jottings to help them. E.g. dots to share out when dividing or bar models to draw out the problem

Abstract-children use just the numbers and symbols

# Concrete and Pictorial

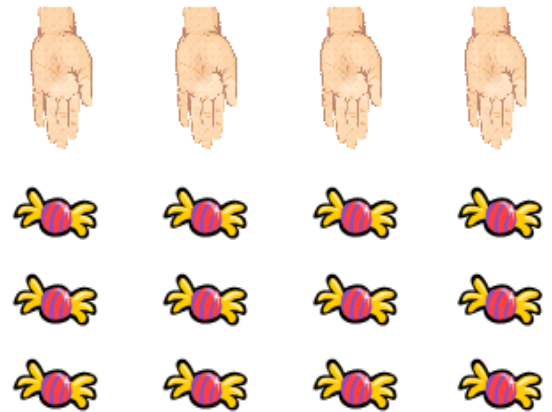
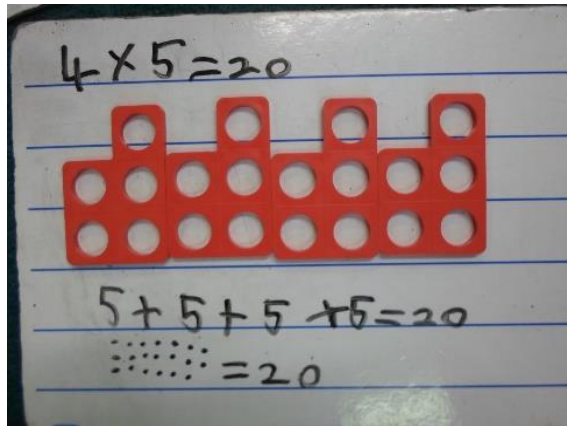
$$46 + 17 = 63$$

T	O
40	6
+ 10	7
60	3
10	

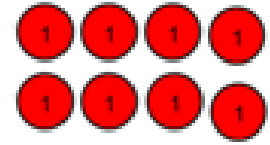


3 groups of 3 = 9  
or  
 $3 \times 3 = 9$

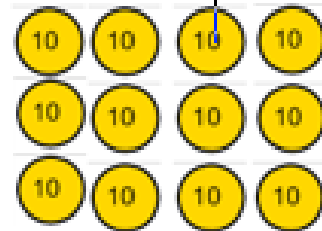
2 groups of 4 = 8  
or  
 $2 \times 4 = 8$



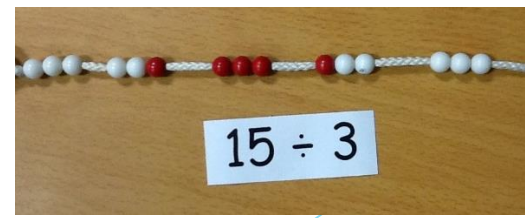
32
X 4
8 (4 x 2)
120 (4 x 30)
200
1





4 x 2

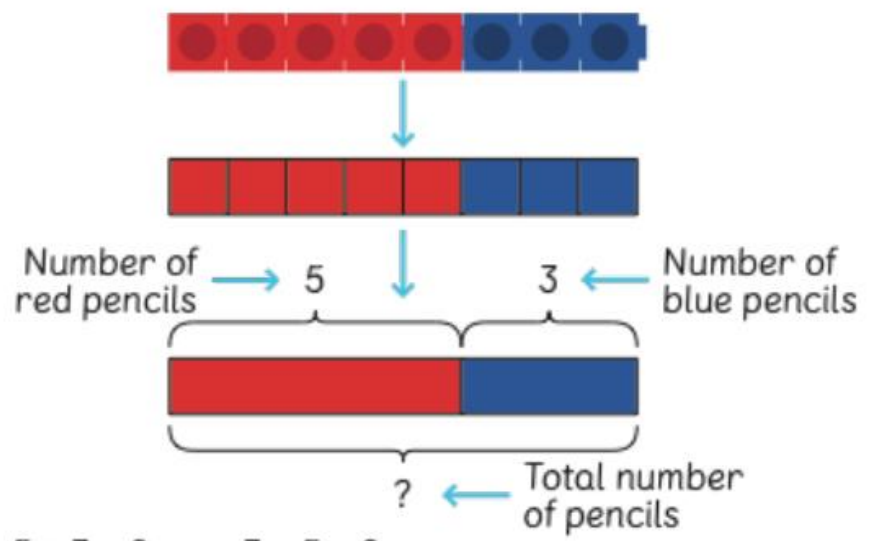


4 x 30



# Moving from concrete to pictorial

1 Use   to show the number of pencils.



$5 + 3 = 8$  or  $3 + 5 = 8$

There are 8 pencils altogether.

Draw bars to show each number.



2



has 15 pencils.

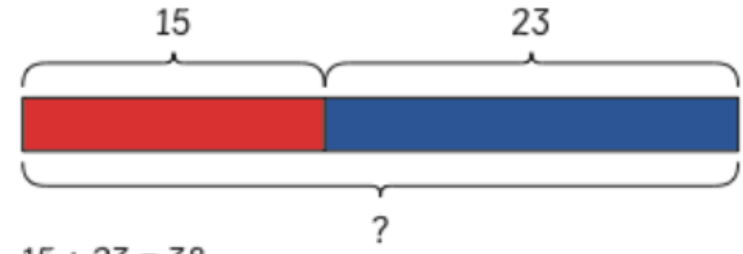


has 23 pencils.

There is not enough space to use   !



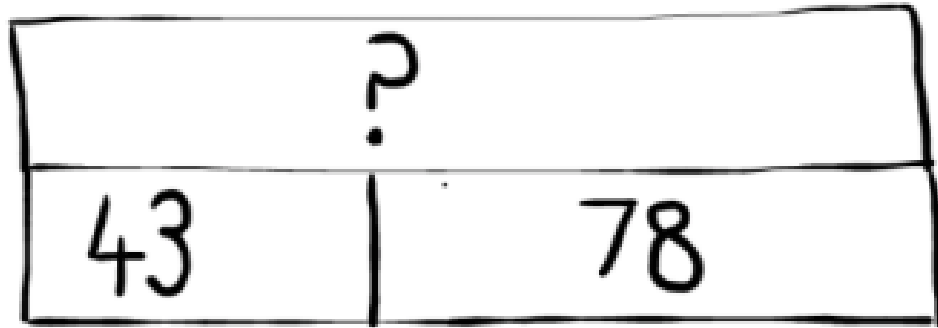
How many pencils do they have altogether?



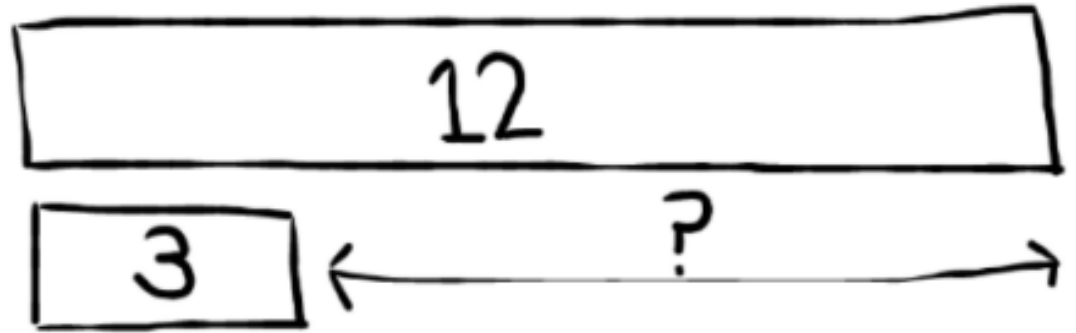
$15 + 23 = 38$

They have 38 pencils altogether.

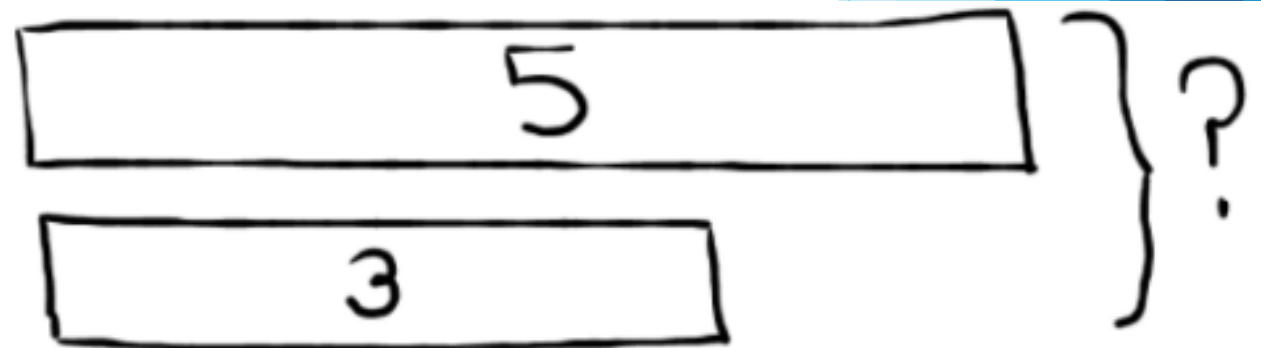
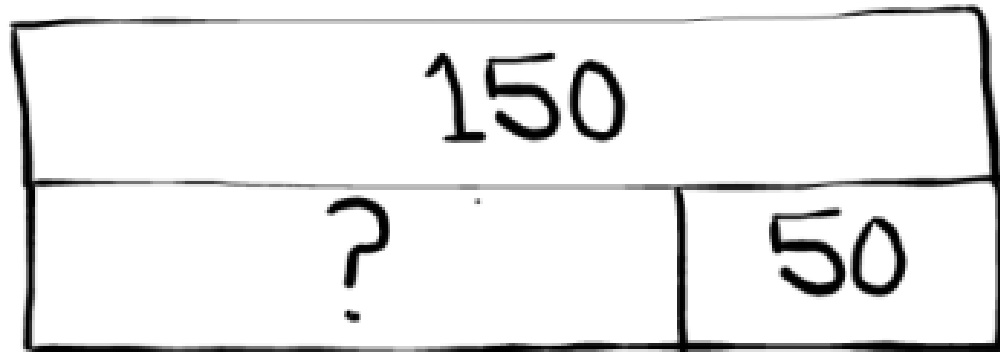
T	O
1	5
+ 2	3
<hr/>	
3	8



Sandi has 12 football cards and Umar has 3. How many more cards does Sandi have than Umar

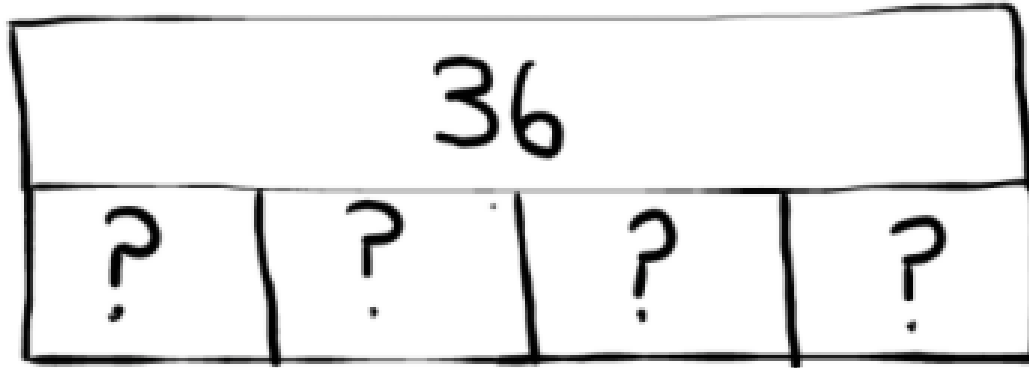


Bar model representing the subtraction equation '150 - 50 = ?'

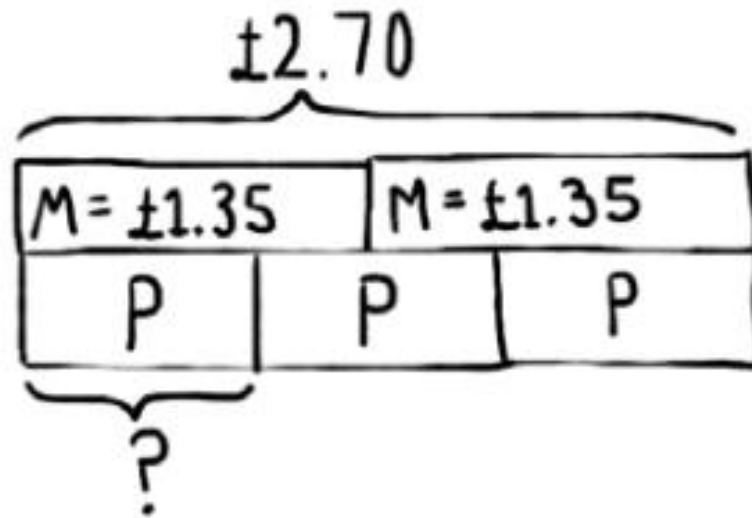




Bar model representing the division equation ' $36 \div 4 = ?$ '  
or the multiplication equation ' $4 \times ? = 36$ '



3 pineapples cost the same as 2 mangoes. One mango costs £1.35.  
How much does one pineapple cost?



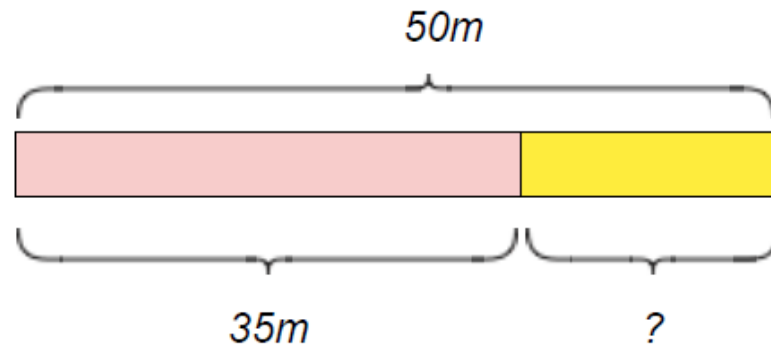


# Bar Method for Subtraction

*Lulu wants to swim 50 metres.*

*She has swum 35m.*

*How far is she from the finishing line?*



*Why do we  
subtract ?*



Seeing a visual representation of the problem helps children develop their conceptual understanding of *why* we need to subtract.

# Problem One:

Sam had 5 times as many marbles as Tom.

If Sam gives 26 marbles to Tom, the two friends will have exactly the same amount.

How many marbles do they have altogether?

Sam

Tom



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If Sam gives 26 marbles to Tom, the two friends will have exactly the same amount.

How many marbles do they have altogether?

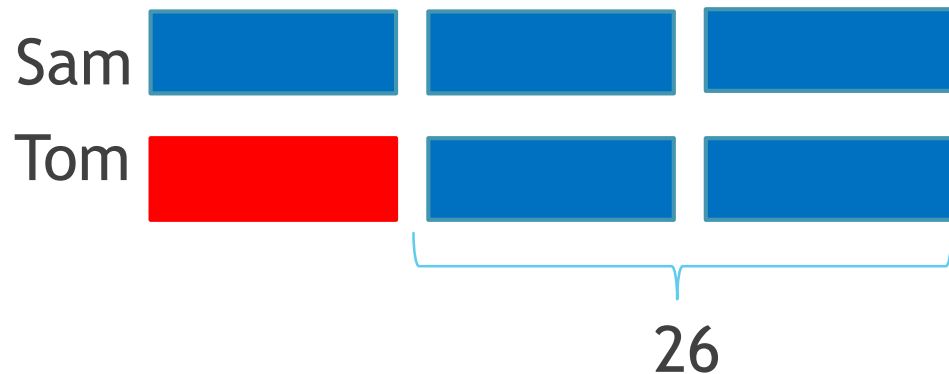


*Children can visually see the need to move two bars down so that Tom and Sam each have the same amount.*

Sam had 5 times as many marbles as Tom.

If Sam gives 26 marbles to Tom, the two friends will have exactly the same amount.

How many marbles do they have altogether?

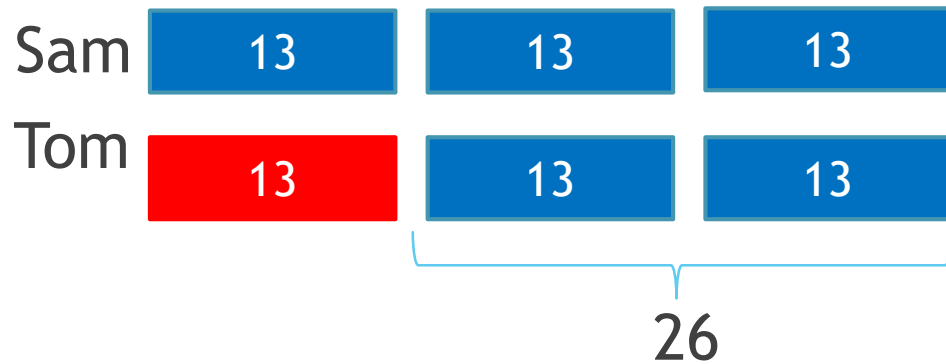


If Sam has given Tom 26 marbles (2 bars) then they can now work out how many 1 bar would be and then go on to complete the question.

Sam had 5 times as many marbles as Tom.

If Sam gives 26 marbles to Tom, the two friends will have exactly the same amount.

How many marbles do they have altogether?



If Sam has given Tom 26 marbles (2 bars) then they can now work out how many marbles 1 bar represents, and then go on to complete the question.  
( $13 \times 6 = \underline{78}$ )

# Bar Models

- ▶ It is a visual model to help children understand a variety of maths problems including addition, subtraction, multiplication, division, fractions, percentages, ratio and algebra.
- ▶ It is *not* a method for solving the problem in itself, but a way or revealing the mathematical structure of a problem (conceptual understanding) i.e. it helps them understand why we need to subtract or divide for example
- ▶ It can help to bridge the gap between using concrete resources and abstract methods.

# Expanded and Compact Methods (+, - and x)

## ▶ Expanded Methods

$$357 + 285$$

$$\begin{array}{r} 300 \quad 50 \quad 7 \\ + 200 \quad 80 \quad 5 \\ \hline \end{array}$$

10 2      or

$$\begin{array}{r} 100 \quad 30 \quad 0 \\ 500 \quad 0 \quad 0 \\ \hline \end{array}$$

$$\begin{array}{r} 600 \quad 40 \quad 2 \\ \hline \end{array}$$

$$\begin{array}{r} 357 \\ + 285 \\ \hline \end{array}$$

$$\begin{array}{r} 12 \\ \hline \end{array}$$

$$\begin{array}{r} 130 \\ \hline \end{array}$$

$$\begin{array}{r} 500 \\ \hline \end{array}$$

$$\begin{array}{r} 642 \\ \hline \end{array}$$

## ▶ Compact Methods

$$357 + 285$$

$$\begin{array}{r} 357 \\ + 285 \\ \hline \end{array}$$

$$\begin{array}{r} 642 \\ \hline \end{array}$$

11



# Expanded and Compact Methods (+ - and x)

## ▶ Expanded Methods

$$876 - 214 = 562$$

$$\begin{array}{r} 800 \quad 70 \quad 6 \\ - 200 \quad 10 \quad 4 \\ \hline \end{array}$$

2 or

60

$$\begin{array}{r} 600 \\ \hline 600 \quad 60 \quad 2 \\ \hline \end{array}$$

$$\begin{array}{r} 876 \\ - 214 \\ \hline \end{array}$$

2

60

$$\begin{array}{r} 600 \\ \hline 662 \\ \hline \end{array}$$

## ▶ Compact Methods

$$876 - 214$$

$$\begin{array}{r} 876 \\ - 214 \\ \hline \end{array}$$

$$\begin{array}{r} 662 \\ \hline \end{array}$$

# Expanded and Compact Methods (+ - and x)

## ▶ Expanded Methods

$$\begin{array}{r} 42 \times 54 \\ \quad 42 \\ \times \quad 54 \\ \hline \quad 8 \quad (4 \times 2) \\ \quad 160 \quad (4 \times 40) \\ \quad 100 \quad (50 \times 2) \\ \underline{2000} \quad (50 \times 40) \\ \hline \underline{2268} \end{array}$$

## ▶ Compact Methods

$$\begin{array}{r} 42 \times 54 \\ \quad 42 \\ \times \quad 54 \\ \hline \quad 168 \\ \underline{2100} \\ \hline \underline{2268} \end{array}$$

# Division

## Short Division

$$864 \div 4$$

$$\begin{array}{r} 216 \\ 4 \overline{) 864} \end{array}$$

$$574 \div 3$$

$$\begin{array}{r} 191 \text{ r } 1 \\ 3 \overline{) 574} \end{array}$$

## Chunking

$$\begin{array}{r} 35 \\ 24 \overline{) 8140} \\ \underline{- 480} \quad (20) \\ 360 \\ \underline{- 240} \quad (10) \\ 120 \\ \underline{- 120} \quad (5) \\ 0 \end{array}$$

## Fact Box

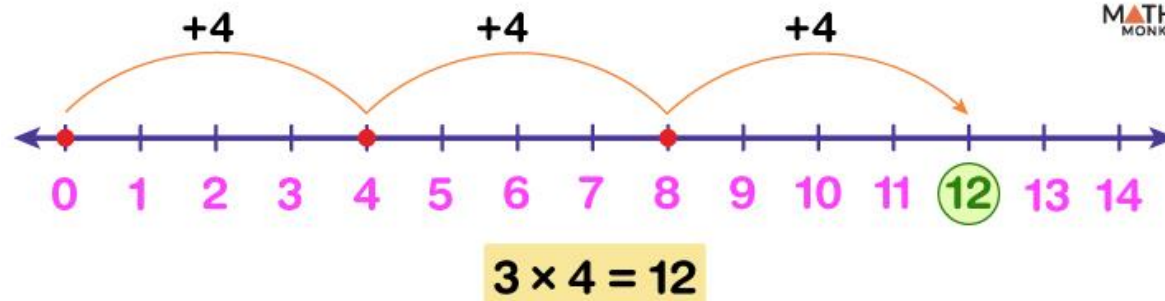
$$24 \times 10 = 240$$

$$24 \times 20 = 480$$

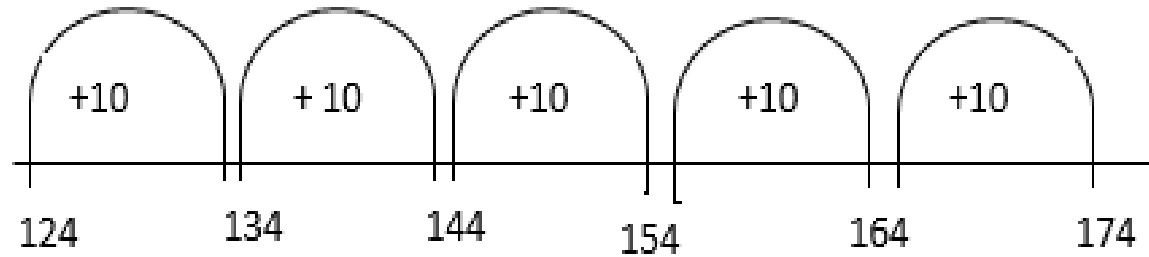
$$24 \times 5 = 120$$

$$24 \times 2 = 48$$

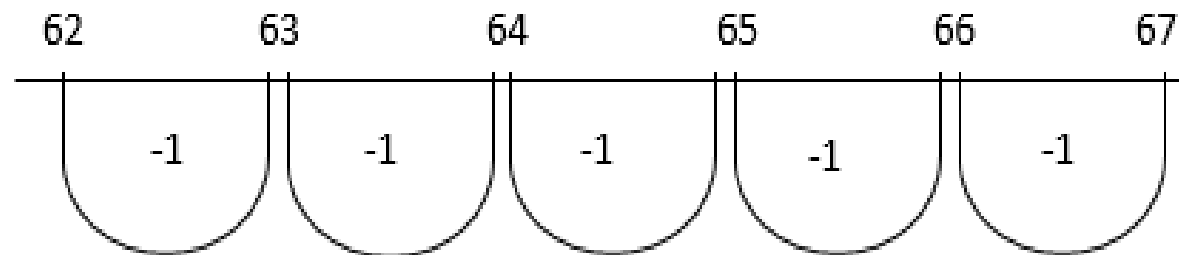
# Number Lines



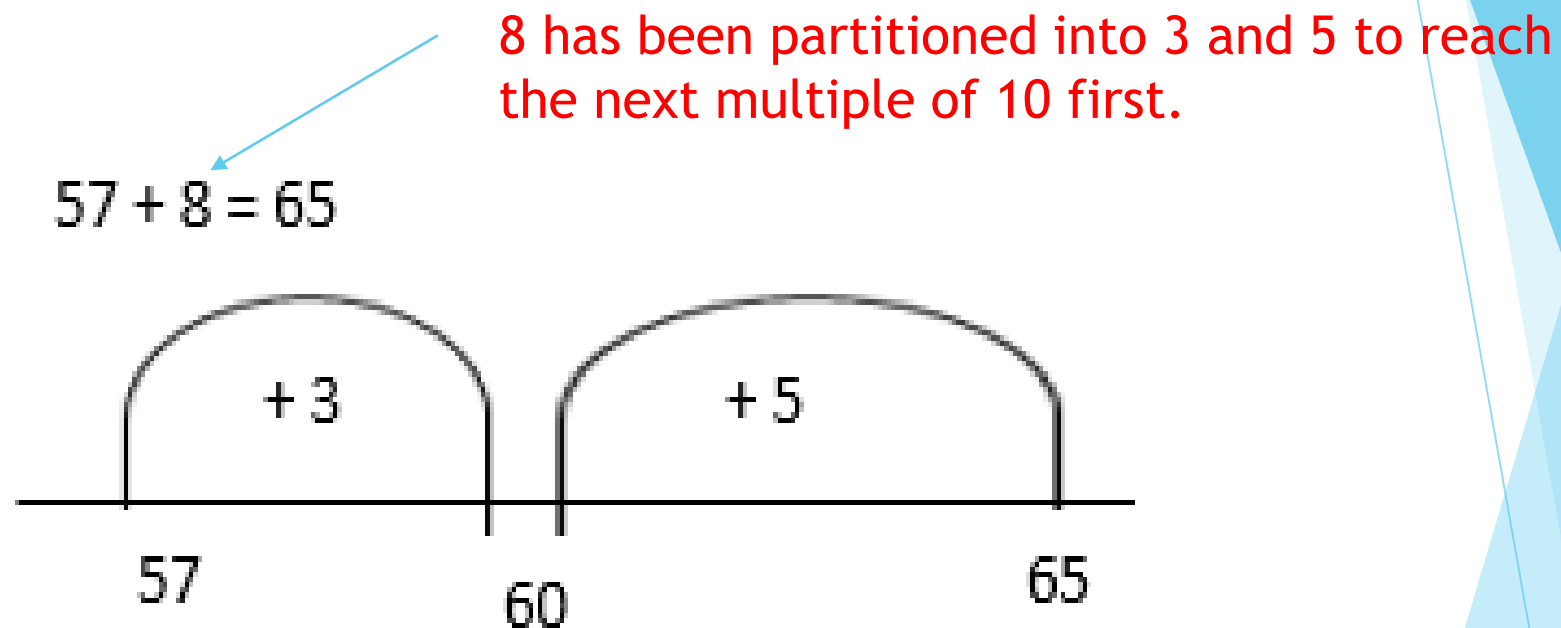
$124 + 50 = 174$



$67 - 5 = 62$



# Partitioning on a number line



# How can you help?

- ▶ Practising the KIRF with your child
- ▶ Supporting your child to learn their times tables-instant recall
- ▶ Encouraging your child to complete the arithmetic homework each week
- ▶ Take a 'little and often' approach to recalling key skills

# Useful websites

**Hit the Button-** <https://www.topmarks.co.uk/maths-games/hit-the-button>

Snappy Maths <http://www.snappymaths.com/multiplication/multiplication.htm>

Time table games: <https://www.timestables.co.uk/games/>

Maths frame: <https://mathsframe.co.uk/en/resources/resource/477/Multiplication-Tables-Check>

TT Rockstars: <https://trockstars.com/>

**BBC Bitesize:** <https://www.bbc.co.uk/bitesize/subjects/z826n39>